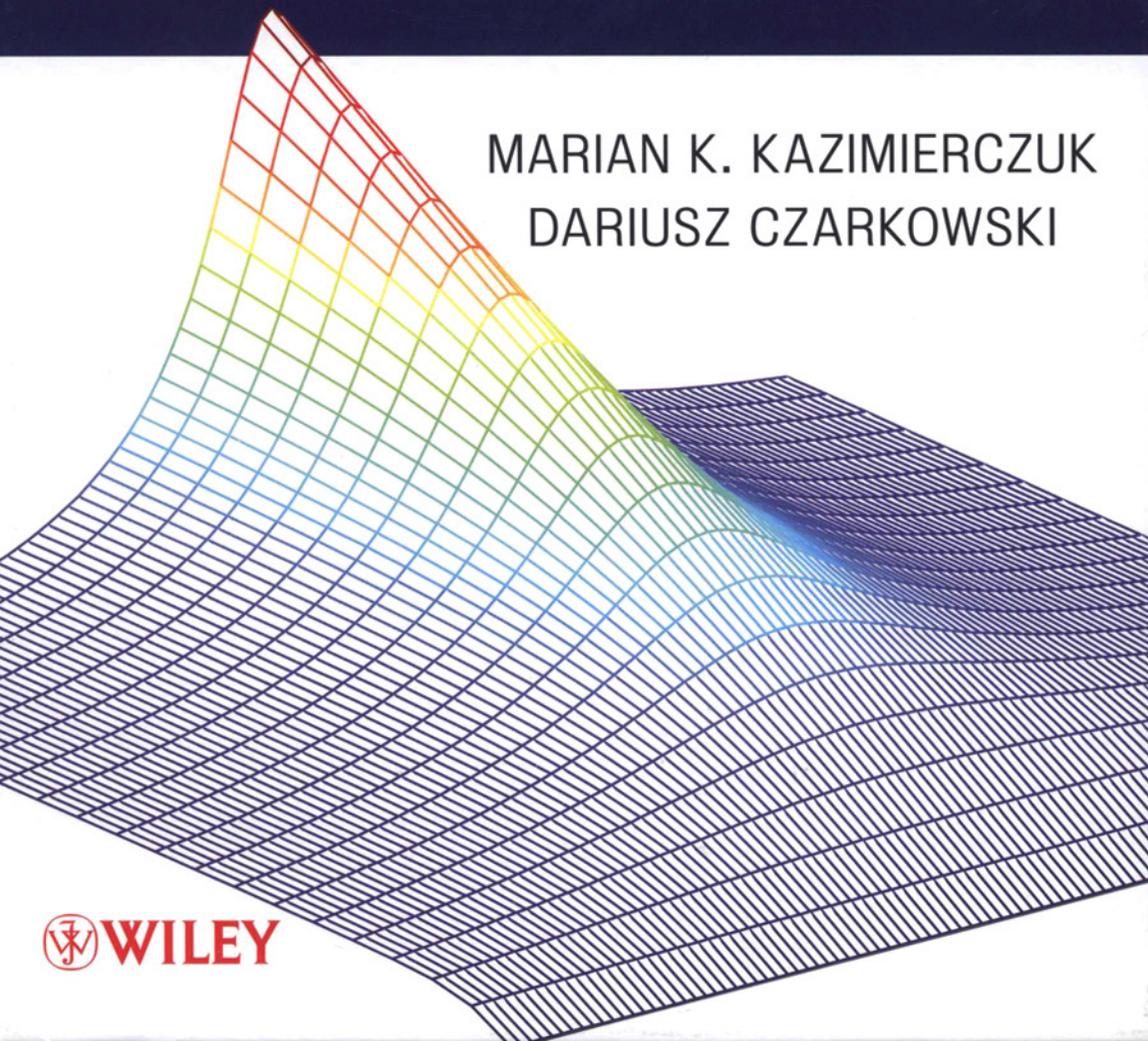


SECOND EDITION



RESONANT POWER CONVERTERS

MARIAN K. KAZIMIERCZUK
DARIUSZ CZARKOWSKI

A 3D surface plot with a grid pattern, colored with a rainbow gradient from red at the peak to blue at the base. It occupies the lower half of the cover.

 **WILEY**

RESONANT POWER CONVERTERS

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Second Edition

Marian K. Kazimierczuk
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Dariusz Czarkowski
Polytechnic Institute of New York University



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To Alicja, Anna, Katarzyna, and Andrzej
To Hanna, Barbara, and Bartosz

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